













$$\begin{aligned} & \mathcal{G}aussian \, \text{Kernel is Separable} \\ & \mathcal{I}_{G} = I * G = \\ & = \sum_{h=-m/2}^{m/2} \sum_{k=-m/2}^{m/2} \mathcal{G}(h,k) I(i-h,j-k) = \\ & = \sum_{h=-m/2}^{m/2} \sum_{k=-m/2}^{m/2} e^{-\frac{h^{2}+k^{2}}{2\sigma^{2}}} I(i-h,j-k) = \\ & = \sum_{h=-m/2}^{m/2} e^{-\frac{h^{2}}{2\sigma^{2}}} \sum_{k=-m/2}^{m/2} e^{-\frac{k^{2}}{2\sigma^{2}}} I(i-h,j-k) = \\ & \text{since} \qquad e^{-\frac{h^{2}+k^{2}}{2\sigma^{2}}} = e^{-\frac{h^{2}}{2\sigma^{2}}} e^{-\frac{k^{2}}{2\sigma^{2}}} \end{aligned}$$













