

Equation

$$\mathbb{E}[p(n+1)|p(n)] = p_1^2(-k_R + k_R C_2 + k_R - k_R C_1 + k_p C_1 - k_p C_2) + p_1(k_R - k_R C_2 + 1 - C_1 - k_R + k_R C_1 - C_2 + 2k_p C_2) + (C_2 - k_p C_2)$$

$k_R = k_p = k$. Quadratics terms disappear

$$\begin{aligned} E[p_i(n+1)|P] &= p_1 \left[-k C_2 + 1 - C_1 + k C_1 - C_2 + 2k C_2 \right] + C_2 (1-k) \\ &= p_1 \left[(1 - C_1 - C_2) + k (C_1 + C_2) \right] + C_2 (1-k) \end{aligned}$$

$$p_i(n+1) \rightarrow p_i^{(\infty)}$$

$$p_i^{(\infty)} \left[- (1 - C_1 + C_2) - k (C_1 + C_2) \right] = C_2 (1-k)$$

$$p_i^{(\infty)} \left[(C_1 + C_2) - k (C_1 + C_2) \right] = p_i^{(\infty)} \left[(1-k) (C_1 + C_2) \right] = C_2 (1-k) \Rightarrow p_i^{(\infty)} = \frac{C_2}{C_1 + C_2}$$